

eg. Carbon 14 has a half-life of 5730 years.

a) what is the decay constant?

$$\lambda = \ln 2 / t_{1/2} = 0.693 / 5730 = 1.21 \times 10^{-4} \text{ a}^{-1}$$

b) what is the probability of a particle nucleus decaying in a year?

$$1.21 \times 10^{-4} \text{ per year}$$

c) you measure a sample and it has an activity of 3.0×10^3 decays per second. How many C 14 atoms are in the sample?

$$dN/dt = -\lambda N \quad N = 3000 \text{ decays/s} / 1.21 \times 10^{-4} \text{ a}^{-1}$$

$$3000 / 0.000121 = 2.479339 \text{E}7$$

$$2.479339 \text{E}7 \times (365.25 \times 24 \times 3600) = 7.824199 \text{E}14$$

$$7.8 \times 10^{14} \text{ atoms}$$

d) if the sample is 40 000 years old (3 sig figs), how many atoms were in the original sample?

$$N = N_0 e^{-\lambda t} \quad N_0 = N / e^{-\lambda t} =$$

$$7.824 \text{E}14 / (e^{(-0.000121 \times 40000)}) =$$

$$9.89 \times 10^{16} \text{ atoms}$$

e) if a sample of C 14 is reduced to 1/32 of the original sample how old is the sample?

$$5 \times 5730 = 28650 = 29 \text{ 000 years old}$$

f) if a sample of C 14 is reduced to 0.000000123453 of the original sample how old is the sample?

$$y = e^x \quad \ln y = x$$

$$N/N_0 = e^{-\lambda t}$$

$$\ln (N/N_0) = -\lambda t$$

$$t = [\ln (N/N_0)] / -\lambda$$

$$t = [\ln(0.000000123453)] / (-0.000121) =$$

$$1.3 \times 10^5 \text{ years old}$$

p1116 problems 17, 25, 57, 59, 65, 69

When anti-matter hits equivalent matter it annihilates - changes into energy.

How much energy? $E = mc^2$

c is speed of light, $3.00 \times 10^8 \text{ m/s}$

When an electron hits a positron (each of mass $9.11 \times 10^{-31} \text{ kg}$) what is the minimum energy of the released photons? Why do I say minimum?

$$E = mc^2 = 9.11 \times 10^{-31} \text{ kg} \times 2 \times (3.00 \times 10^8 \text{ m/s})^2$$
$$= 1.64 \times 10^{-13} \text{ J}$$

$$\text{MeV} = 1.602 \times 10^{-13} \text{ J (alternate units)}$$

$$\text{so } E = 1.0 \text{ MeV}$$

The released photons must obey conservation laws:

conservation of energy, energy of the photons = mass energy + kinetic energy

conservation of momentum - so the momentum of

the photons $p = h/\lambda = hf/c$ must equal the momentum of the electron and positron.

Binding energy

The mass of a proton is 1.007276u

the mass of neutron is 1.008665 u

u is the atomic mass unit, $1u = 1.661 \times 10^{-27} \text{kg}$
defined as 1/12 the mass of a carbon 12 nucleus.

Hey, wait.

Carbon 12 = 12.000000000000000000000000 u

but Carbon 12 is 6 protons and 6 neutrons

$6 \times (1.007276) + (6 \times 1.008665) = 12.095646 \text{ u}$

What's the deal?

where did the $12.095646 - 12 = 0.095646 \text{u}$ of mass go?

Nuclear Fusion in stars is where small nuclei fuse together to form bigger nuclei and give off lots of energy. Where did the energy come from? The mass lost between the reactants and products of the reaction.

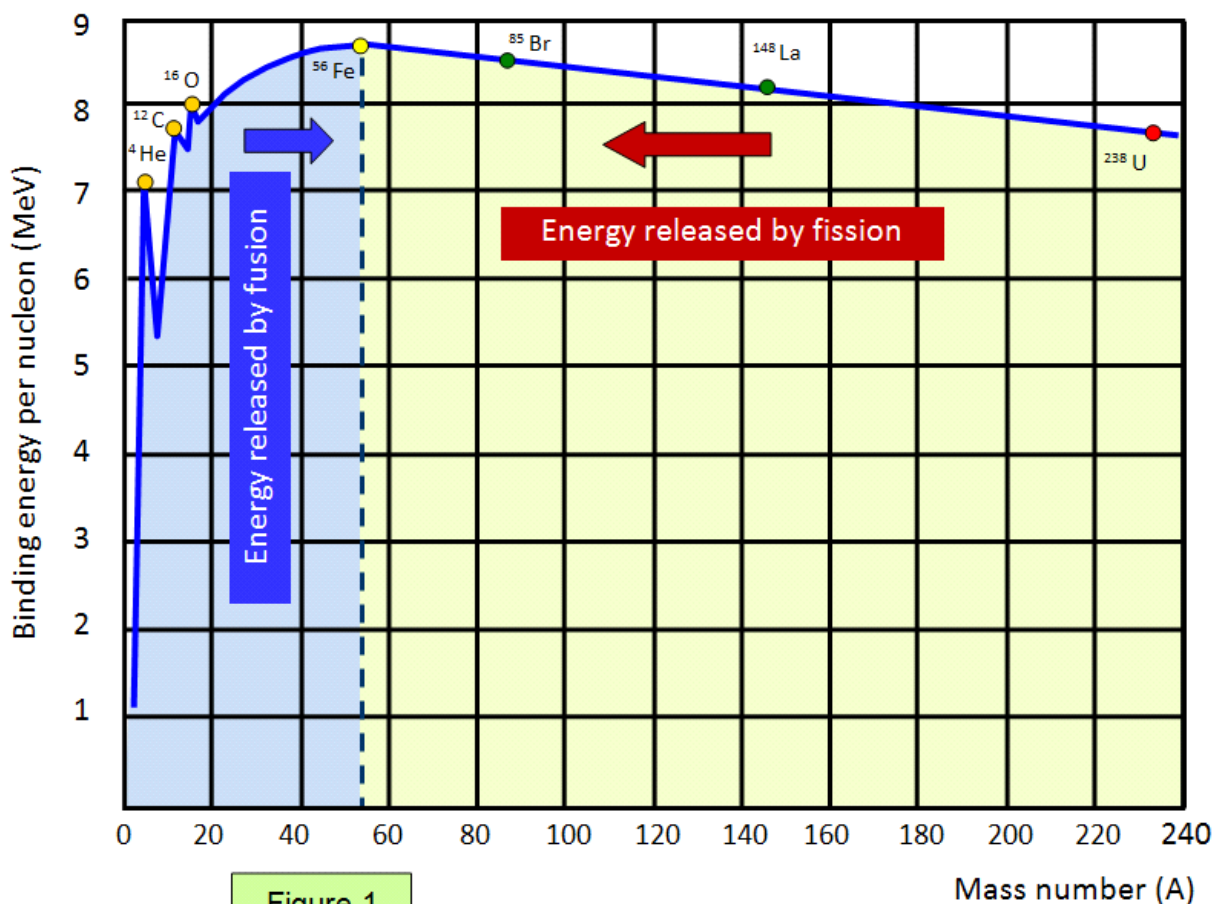
Binding Energy - energy released when a nucleus is formed from constituents. It is also the energy required to pull the nucleus apart into its constituents.

Calculate the Binding energy = mass defect in u x conversion factor 931 MeV/u.

for Carbon 12 mass defect = $12.09564 - 12 = 0.09564 \text{ u}$

Binding energy = $0.09564 \times 931.5 = 89.0 \text{ MeV}$

(derive 931.5 MeV/u from $E=mc^2 = 1.661 \times 10^{-27} \text{ kg} \times (2.9979 \times 10^8 \text{ m/s})^2 = 1.661 \times 9 = 14.949 \times 10^{-11} \text{ J} / 1.602 \times 10^{-13} \text{ J/MeV} = 931.5 \text{ MeV}$ for every u)



Note the Fe56 is given as the highest binding energy per nucleon - Fe56 is the largest nucleus produced in stars - larger atoms are produced in supernovae

Fission is when large nuclei break into 2 smaller daughter nuclei.

Fissionable materials: Uranium 235, used for Hiroshima bomb and in most nuclear reactors. Plutonium 239 was used in Nagasaki bomb and most modern nuclear bombs. Not natural, created by bombarding uranium 238 with neutrons.

In nature Uranium is mostly uranium 238, and enriching uranium by separating 235 from 238 is difficult because they have the same chemical properties.

Thorium can be fissionable if bombarded with neutrons - good candidate because it is cheap and plentiful and harder to make into a bomb.

eg. What is the binding energy of tritium, isotopic mass of 3.01602931u (tritium is H 3, 2 neutrons one proton)?

From https://www.google.ca/webhp?sourceid=chrome-instant&ion=1&espv=2&ie=UTF-8#q=isotopic+mass+of+tritium&*>

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Problem 26,27,28,29, 41, 47, 52, 75

$$\left[1(1.007276) + 2(1.008665) \right] - (3.01602931) \left(\frac{931.5 \text{ MeV}}{1 \text{ u}} \right)$$

$$= (30160293) \text{ J} / 1000000000 \text{ J} = 0.030160293$$

$$= 7.989 \text{ MeV}$$

$$\text{binding energy/nucleon} = 7.989/3 = 2.663$$